

Linear Algebra Introduction

Preston Pan

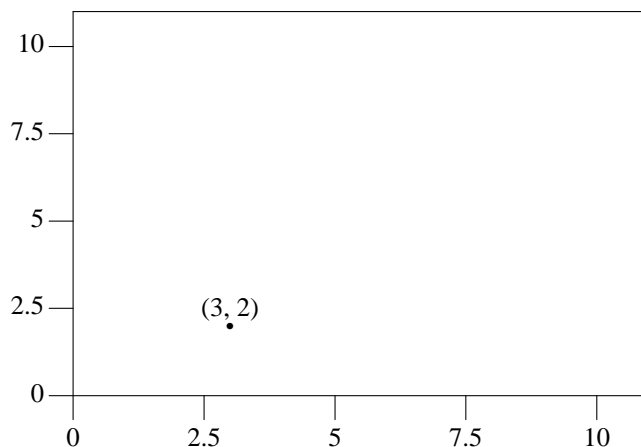
Pacific School of Science and Inquiry

Linear algebra is a subject that is worthy of studying if you are looking to analyze data in any systematic way, or if you are attempting to represent multidimensional (or multivariable) quantities in a structured way. Therefore, everyone in STEM and even in the social sciences should know about linear algebra and a little bit of the mathematical theory behind it.

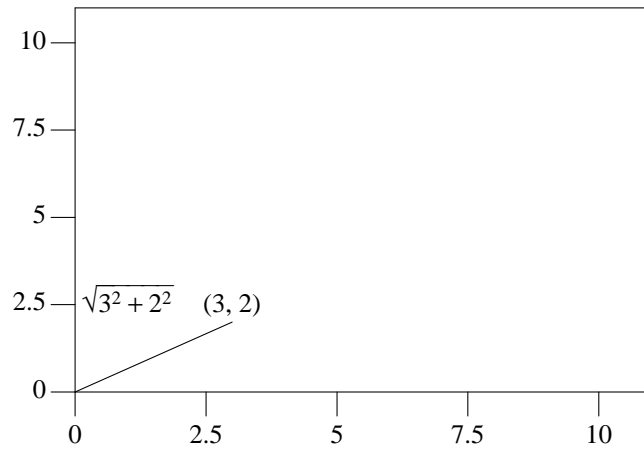
I will be introducing subjects regarding linear algebra from the perspective of physics, though you do not need to know much physics in order to understand most of my explanations.

You might know that in high school physics, all the equations are introduced as one dimensional equations (that is to say, most equations that are introduced only work if the object or objects in question only move forwards and backwards, or any other singular direction). Of course, in real life, there are at least three spatial dimensions, so one dimensional equations just won't model real life well. In these scenarios, it is useful to consider linear algebra as a systematic way to represent direction and motion in three dimensions. With this motivation, we start investigating.

One way we can represent two dimensional space is with a coordinate system. For example, we can have a point $(3, 2)$ which represents a single point three units right and two units up in a coordinate system.



Now, let's imagine that this point $(3, 2)$ represents a force in a certain direction. For example, we can draw a line from the origin to this point and the resulting force's magnitude will be represented by the length of the line in question (which can be obtained via the pythagorean theorem), and the direction of the force will be outwards from the origin following the line.



We can now imagine another line segment drawn from the origin $(-1, 3)$, which we can imagine to be another force acting in a different direction with a different magnitude:

